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TECHNICAL REPORT BRL-TR-3181

**BRL**

THE MECHANICAL RESPONSE OF M30, XM39,  
AND JA2 PROPELLANTS AT STRAIN RATES  
FROM  $10^{-2}$  TO  $250 \text{ SEC}^{-1}$

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JANUARY 1991

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## 1. INTRODUCTION

The mechanical response of gun propellant is of interest to interior ballisticians since fracture damage can adversely affect the mass generation rate during the ballistic cycle. Three macroscopic fracture mechanisms have been identified which include: 1) perforation rupture (hydraulic fracturing), 2) direct grain impact, and 3) intergranular contact stress<sup>1</sup>. To the author's knowledge, the phenomenon of perforation rupture in gun propellant has not been experimentally investigated by interior ballisticians although hydraulic fracture studies are common in the rock mechanics literature<sup>2</sup>. Interior ballisticians have investigated fracture by direct grain impact using a Gas Gun Impact Tester<sup>3</sup> (GGIT), Drop Weight Mechanical Properties Tester<sup>4</sup> (DWMPT), Split Hopkinson Bar Apparatus<sup>5</sup> (SHB), and most recently a new High Rate MTS Systems Corporation Servohydraulic Tester (MTS) which will be discussed in more detail later. Intergranular contact stress fracture phenomena have been investigated with a variety of bed testers<sup>6,7,8</sup> and are primarily devoted to evaluating the bulk response of the propellant bed.

The pressure, temperature, and strain history induced in a propellant bed during ignition and combustion can be severe and complex; x-ray methods<sup>9,10</sup> and in situ pressure pulse monitoring methods<sup>11</sup> provide estimates of operational strain rates that approach  $10^4 \text{ sec}^{-1}$  and peak pressures that approach 700 MPa<sup>12</sup>. Operating temperatures will vary with climate and typically range from -46° to 63° Celsius. Over this temperature range, a brittle-ductile transition in propellant response might be observed as in many materials whose deformation mechanisms are thermally activated.

One objective of propellant testing programs is to relate single grain mechanical property data such as compressive modulus, absorbed strain energy density, yield stress or strain, et cetera, to the combustion characteristics (primarily the mass generation rate) of the deformed propellant. The studies aim to determine if fracture generated surface area is responsible for catastrophic failure and breech-blow phenomena that sometimes occur during gun firing. Characterization of a material's mechanical response might also aid in survivability studies of armored weapons systems which are vulnerable to various forms of attack. An ancillary experimental objective is to provide material property data for use in numerical hydrodynamic simulations of the ballistic process.

This report describes the mechanical property test results obtained for the room temperature, uniaxial compressive deformation of M30, XM39 and JA2 gun propellants at strain rates from  $10^{-2}$  to 250 per second using the Ballistic Research Laboratory's new servohydraulic mechanical properties tester. Also included are comparisons with data obtained on the Split Hopkinson Bar Apparatus and Drop Weight Mechanical Properties Tester. Finally, a preliminary viscoelastic characterization of the gun propellant provides relaxation moduli, secant moduli, and a test for "material" linearity/nonlinearity.

## 2. SERVOHYDRAULIC APPARATUS AND DATA ACQUISITION

The High Rate MTS 310 Material Test System (Figure 1) consists of a conventional two-pole press with a servohydraulically actuated ram that operates from quasistatic velocities to a maximum velocity which approaches 12 m/sec; the maximum velocity imparts a maximum strain rate of 1200  $\text{sec}^{-1}$  on a 10 mm long specimen. Other essential components include a bell and cone piston assembly which permit fixed amounts of total specimen strain, a lower  $\text{N}_2$ -spring piston designed to absorb the impact shock, a 60 kN Kistler force gage mounted in the upper moving piston, and an externally mounted LVDT for displacement measurement. A Thermotron conditioning oven/refrigerator surrounds both upper and lower pistons and permits temperature testing from  $-85^\circ$  to  $90^\circ$  Celsius. Arbitrary load and/or displacement histories can be imparted to the specimen by computer control. Raw force and displacement data are acquired, stored, and then analyzed with a Norland 3001 data acquisition system. Finally, plots of stress and strain versus time, and stress versus strain are printed on a Dataproducts dot matrix printer via RS232 port. The data can also be uploaded via RS232 port

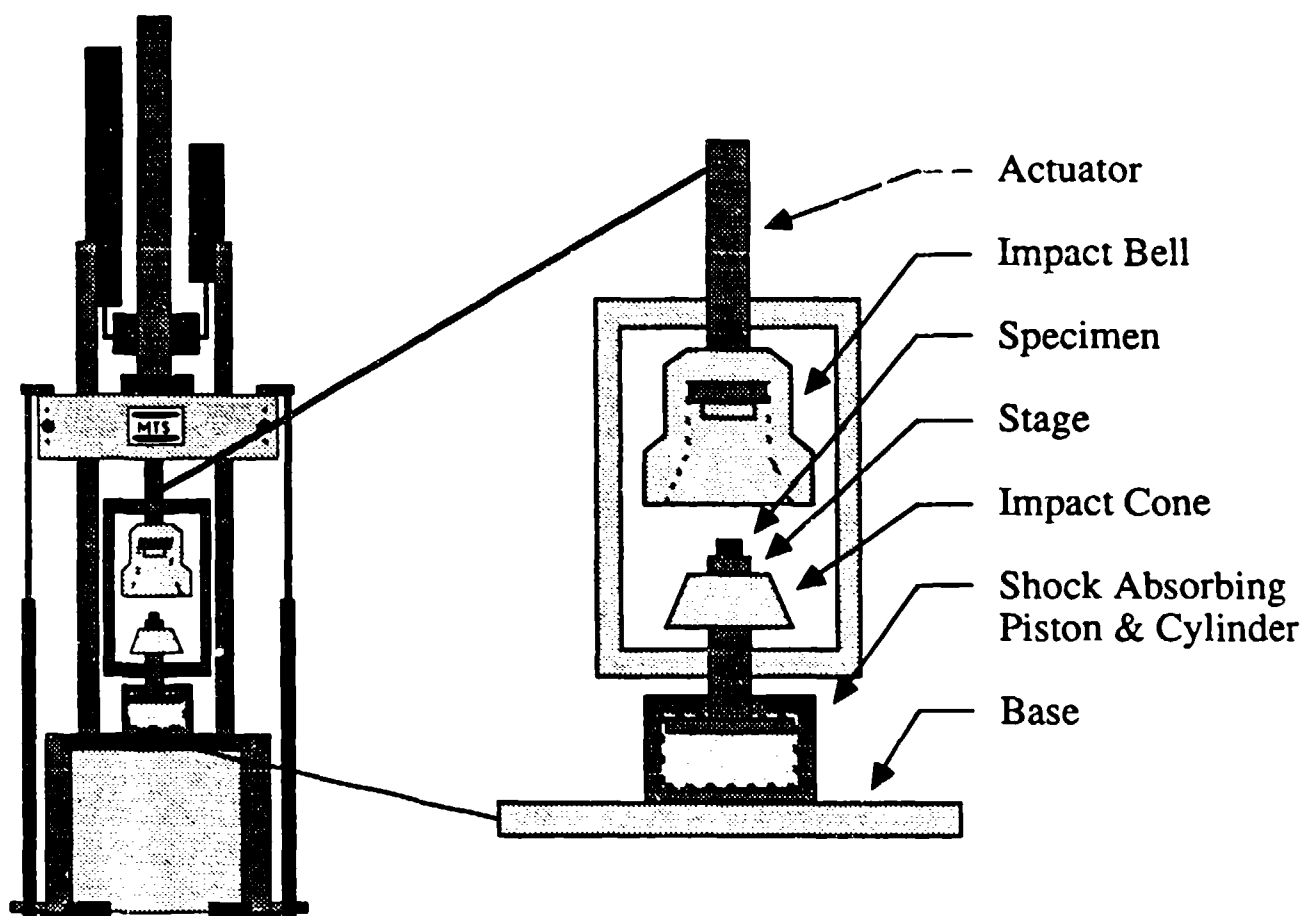


Figure 1. Servohydraulic Test Apparatus with Upper Bell and Impact Cone Piston Assembly.

to a PC and converted to ASCII format for more sophisticated analysis.

The 60 kN Kistler force gage is calibrated every 2 to 3 months using a Morehouse Ring Dynamometer (S/N M-4644); the instrument is certified by the National Bureau of Standards to have an uncertainty to within .003 percent of the applied load. The maximum uncertainty in force measurement is 2 percent and is determined by comparing the force readings from the Dynamometer with the amplified signal on the Norland data acquisition system. The uncertainty in the displacement measurement is within 1 percent as determined by comparison with a National Bureau of Standards certified displacement dial gage (personal communication with Aaron Anderson, MTS Project Engineer).

**2.1 Apparatus Stiffness.** A mechanical idealization of the deformation apparatus (Figure 2) assumes that all machine components are linearly elastic. Contact nonlinearities due to interface mismatch are disregarded. The apparatus idealization consists of three spring components in series.  $K_{mu}$  represents the upper machine stiffness and consists of stiffness contributions from the upper piston, the actuator, the hydraulic fluid, the crosshead and tie rods.  $K_s$  represents the specimen stiffness.  $K_{ml}$  represents the lower machine stiffness and consists of stiffness contributions from the lower piston, the  $N_2$ -filled pressure vessel, and the load unit base. The force is assumed to be the same in each spring, however the displacements in each spring will vary according to their individual stiffnesses.

In a typical test, the measured displacement,  $d$ , must be corrected for stiffnesses  $K_{mu}$  and  $K_{ml}$  in order to accurately calculate the displacements in the specimen. Fortunately, gun propellants are relatively soft in comparison to the apparatus so that the correction is not very large. We can lump

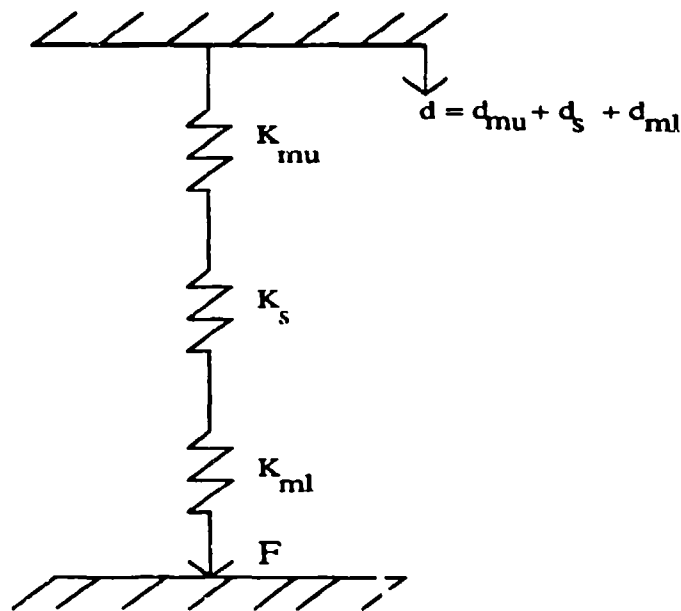


Figure 2. Mechanical Idealization of the MTS using a Linear Elastic Spring Model.

together the  $K_{mu}$  and  $K_{mj}$  stiffness contributions and arrive at an apparatus stiffness  $K_a$  according to the equation:

$$1/K_a = 1/K_{mu} + 1/K_{mj} \quad (1)$$

where the total system stiffness  $K$  is given by:

$$K = 1/(1/K_a + 1/K_s) = F/d \quad (2)$$

where

$F$  = total measured force

$d$  = total measured displacement

The apparatus stiffness is determined by performing an experiment using a specimen whose stiffness  $K_s$  is very large and hence negligible relative to the ratio  $1/K_a$ . A set of seven experiments was conducted using a hardened steel slug and the average apparatus stiffness was determined to be  $K_a = 91.87 \pm 4.8$  kN/mm.

**2.2 Stored Elastic Strain Energy.** The amount of elastic strain energy,  $W$ , stored in a cylindrical elastic rod under applied force,  $F$ , is given by:

$$W = F^2/2K \quad (3)$$

where the stiffness,  $K$ , is given by:

$$K = AE/L \quad (4)$$

where

$L$  = rod length

$A$  = rod area

$E$  = Young's modulus

We can determine how the elastic strain energy,  $W$ , is partitioned between the apparatus and a propellant grain during compression by first determining a "typical" propellant grain stiffness. The stiffness of a grain of XM39 at  $250 \text{ sec}^{-1}$  with crosssectional area,  $A = 24.5 \text{ mm}^2$ , length,  $L = 6.5 \text{ mm}$ , and compressive modulus,  $E = 3.5 \text{ GPa}$ , is  $K = 13 \text{ kN/mm}$ . At a strain rate of  $250 \text{ sec}^{-1}$ , XM39 yields at about 47 MPa or an axial force,  $F = 1.15 \text{ kN}$ . Hence from Equation 3 the elastic energy stored within the grain at yield is .051 kN-mm. Using the apparatus stiffness and Equation 3 we see that the energy stored in the apparatus at yield is .0072 kN-mm which is 7 times less than the elastic strain energy stored in the specimen, or only 12 percent of the total system elastic strain energy.

This observation has important consequences for studying the post-failure response of gun propellant since in stiff testing machines the elastic strain energy present in the apparatus is negligible relative to the specimen and failure of the specimen can proceed under stable conditions. Jaeger and Cook<sup>2</sup> regard the failure process as being stable if the post-failure material stiffness is less than that of the apparatus. Under these conditions the complete stress-strain curve can be cap-

tured. However, in soft testing machines the elastic strain energy stored in the apparatus is violently released during specimen failure and hence the complete post-failure response of the specimen cannot be obtained.

Specimen failure for brittle materials is defined<sup>2</sup> in the classical macroscopic sense as a continuous process that begins at the maximum stress (point where the tangent modulus of the stress-strain curve is zero) and continues for an indefinite period (tangent modulus of the stress-strain curve is negative) until ultimate failure or the complete loss of load bearing capacity occurs (Figure 3). If ultimate failure occurs at relatively small strains the material is termed brittle. Ductile materials ultimately fail at relatively large strains and can be accompanied by significant workhardening behavior. It is important for interior ballisticians to be able to identify when a particular propellant begins to fracture, since it is at this time that additional surface area becomes available for burning. However, by examining stress versus strain curves alone, no information can be obtained regarding the mechanism of deformation whether it be fracture, compaction, crystal plastic flow, bond stretching,

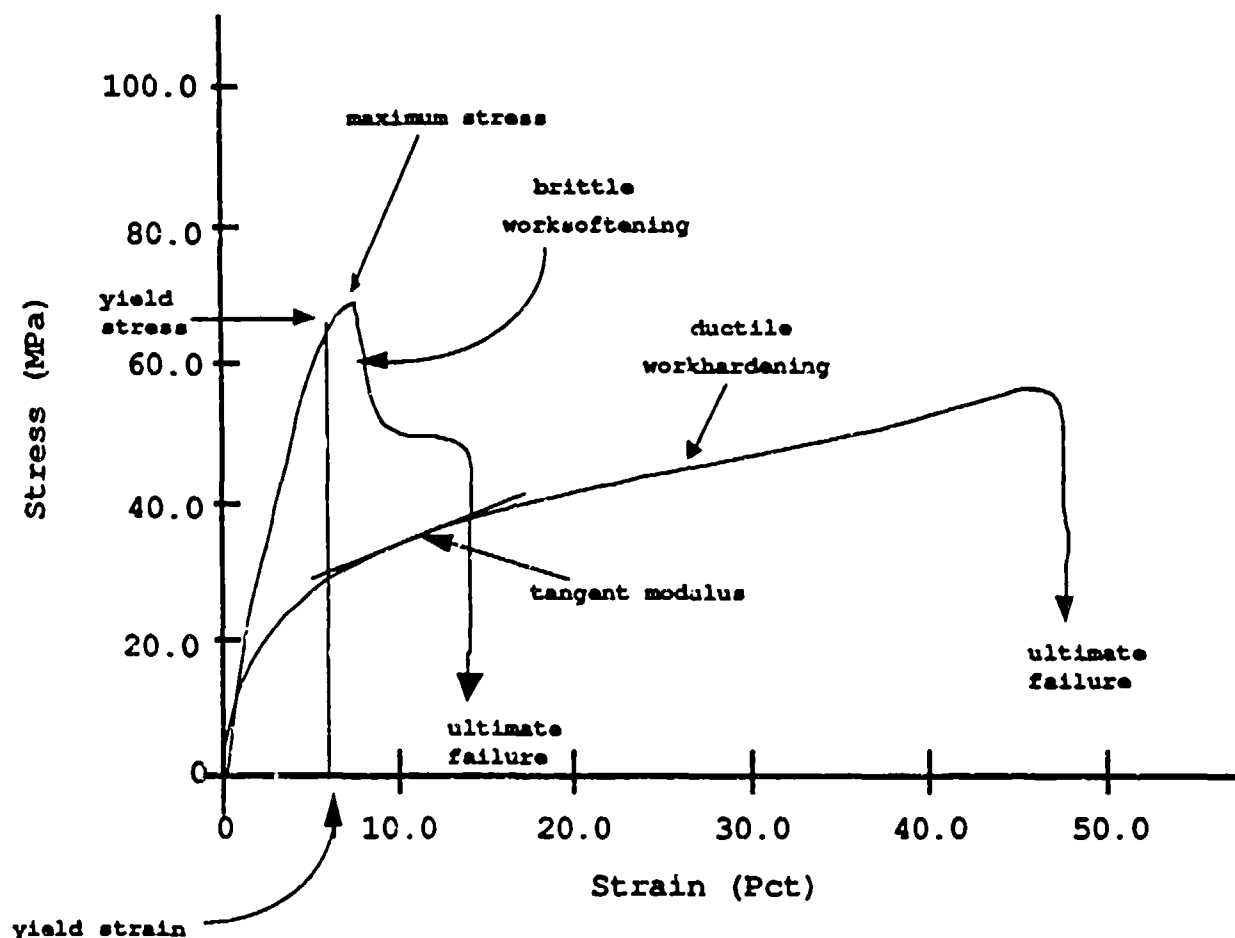


Figure 3. Macroscopic Brittle-Ductile Response for Materials.

et cetera, or how the relative contributions of the mechanisms are partitioned in pressure, temperature, and strain space. Deformation by fracture can be identified by detailed micromechanical observation, using, for example, the scanning electron microscope or optical microscope. Once fracture has been identified as a dominant deformation mechanism for a particular propellant then an important experiment would be to perform a series of tests where different specimens are deformed to increasing amounts of fixed total strain at various strain rates and temperatures; the new servohydraulic test apparatus has this capability because of its unique bell and cone impact housing design. The deformed grains could then be burned in a mini-closed bomb<sup>1</sup> and the combustion characteristics (burning rate, mass generation rate, et cetera) could be quantitatively related to one or more gross mechanical property parameters. Research is presently under way to investigate the effects of strain rate, temperature, and degree of fixed axial strain on the mass generation rate and burning rate of M30 and JA2 propellants.

### 3. EXPERIMENTAL PROCEDURE

Right circular cylinders of M30, XM39, and JA2 (abbreviated lots are 67878, 1333, and S110 respectively) are cut from granular propellant stock using an Isomet diamond saw. Care is taken to cut the ends parallel to each other and perpendicular to the cylinder axis so that the compressive deformation is coaxial and uniform. Specimen dimensions are measured with a vernier caliper and length to diameter ratios (L/D) average about 1:1 (Table 1) for each of the propellant formulations<sup>13</sup> (Table 2).

Table 1. Average Lengths, Diameters, and Perforation Diameters of Propellant Specimens.

	Length (mm)	Diameter (mm)	L/D	Perf.-Diam. (mm)
M30	9.581 ± 0.34	7.042 ± 0.059	1.361	.686
XM39	6.929 ± 0.37	5.643 ± 0.046	1.228	.305
JA2	9.091 ± 0.43	8.719 ± 0.068	1.043	.483

Table 2. Percent Composition of JA2, M30, and XM39 Gun Propellants.

Propellant	JA2	M30		XM39
Component	%	%	Component	%
Nitrocellulose	59.0	28.0	RDX (ground)	76.0
NC Nitration Level	13.0	12.6	Cell. Acetate Butyrate	12.0
Nitroglycerin	15.0	22.0	Acetyl Triethyl Citrate	7.6
Nitroguanidine	0.0	48.0	Nitrocellulose	4.0
Ethyl Centralite	0.0	2.0	NC Nitration Level	12.6
Diethylene Glycol			Ethyl Centralite	0.4
Dinitrate	25.0	0.0		
Akardit II	1.0	0.0		

All tests are performed at ambient pressure (0.1 MPa) and temperature (22° Celsius). Molybdenum disulphide,  $\text{MoS}_2$ , is applied sparingly to the specimen ends prior to testing in order to reduce frictional end effects and specimen barreling. A minimum of five specimens are deformed to 50 percent strain, at nominal strain rates of .01, 1, 100, and 250 per second.

**3.1 Data Reduction.** The raw force and displacement data are reduced and converted to stress versus strain plots as previously reported<sup>13</sup>. Two additions to the standard data reduction program include an apparatus distortion correction and an algorithm for automatically picking the yield stress. The net axial stress is determined using the initial cross-sectional area of the specimen minus the perforation area. In future work, a stress correction due to increasing cross-sectional area of the specimen can be made after the Poisson's ratio is determined using a lateral deformation gage. The raw force and displacement voltages versus time, stress and strain versus time, calibration factors, specimen dimensions, and the following mechanical parameters are calculated and stored on floppy disks: maximum stress, stress and strain at yield, strain rate, compressive modulus, strain energy density absorbed per unit volume at yield, strain energy density at selected strain increments past yield, ratios of subsequent strain energy density values relative to the strain energy density at yield. Macroscopic yield is defined<sup>5,13</sup> as the stress level where the material most rapidly loses its ability to sustain load; the yield stress level is determined by finding the minimum in the second derivative of stress with respect to time. Since the second derivative data is somewhat noisy, an n-point smoothing algorithm is used so that a consistent, operator-independent criterion exists for picking the minimum. Equally arbitrary definitions of the yield point, such as the proportional limit definition (stress level at the end of the linear range) or offset method definition (stress level after 0.2 percent offset strain), were not viable candidates since for the former definition a suitable linear range is difficult to determine for these materials and for the latter definition the yield would occur at fractions of a percent of maximum stress and the strain dependence of yield could not be investigated. The choice of the yield point, as it relates to strength loss due to fracture, should ultimately be constrained by microphysical considerations.

**3.2 Grain Geometry Effects.** Each of the propellant grains contains seven perforations so that during axial compression a highly inhomogeneous stress field could develop due to internal stress concentrations and noncoaxiality of the perforations with the grain axis. The results of this study provide data regarding the mechanical or structural response of propellant grains which are useful for evaluating how grains might behave during axial impact in a gun cartridge. In order to determine material or constitutive properties of gun propellant, for use in numerical simulations of the ballistic process, tests on solid propellant grains could be performed in order to ensure homogeneity of the stress field within the specimen. The determination of material properties is necessary in order to predict the location and intensity of pressure instabilities due to fracturing in a propellant bed. A future study is planned to evaluate the degree to which the propellant response is affected by grain geometry. This will include a study of the propellant response by varying the length to diameter ratio, solid versus perforated grains, lubricated versus unlubricated end conditions, multiaxial stress states including compression, tension and possibly torsion.

#### 4. EXPERIMENTAL RESULTS

Summaries of the experimental results for the uniaxial compression of M30, XM39 and JA2 as a function of strain rate appear in Tables 3,4,and 5 respectively. Synoptic plots of axial stress versus strain as a function of strain rate, reveal that M30 and XM39 reach a maximum stress and then work-soften in response to a constant strain rate input (Appendix A). JA2 responds by continually work-hardening throughout its deformation history. All three propellants behave in a macroscopically ductile fashion and sustained over 40 percent axial shortening.

Table 3. JA2 Servohydraulic Compression Test Results. Y is the Yield Point and is defined as the Stress Level Which Corresponds to the Minimum in the Second Derivative of Stress with Respect to Time.

	Nominal Strain Rate (sec <sup>-1</sup> )		
	10 <sup>-2</sup>	1	100
Max. Stress (MPa)	22.65 ± 1.30	37.75 ± 6.35	61.69 ± 2.62
Stress @ Y (MPa)	4.49 ± 0.64	9.26 ± 1.73	14.45 ± 1.58
Strain @ Y (%)	3.48 ± 0.75	3.25 ± 0.59	3.06 ± 0.37
Strain Rate (sec <sup>-1</sup> )	.0098 ± .001	0.97 ± 0.04	92.06 ± 15.27
Modulus (GPa)	0.19 ± 0.03	0.41 ± 0.11	0.77 ± 0.19
Energy @ Y (MPa)	0.06 ± 0.02	0.12 ± 0.05	0.15 ± 0.02
	200	250	
Max. Stress (MPa)	77.96 ± 11.81	72.29 ± 9.26	
Stress @ Y (MPa)	18.30 ± 1.38	17.30 ± 1.50	
Strain @ Y (%)	3.05 ± 0.84	3.23 ± 0.63	
Strain Rate (sec <sup>-1</sup> )	200.30 ± 8.21	244.50 ± 3.32	
Modulus (GPa)	0.77 ± 0.08	0.79 ± 0.09	
Energy @ Y (MPa)	0.24 ± 0.07	0.21 ± 0.05	



Table 4. M30 Servohydraulic Compression Test Results.

	Nominal Strain Rate (sec <sup>-1</sup> )			
	10 <sup>-2</sup>	1	100	250
Max. Stress (MPa)	41.07 ± 28.82	51.41 ± 2.78	94.55 ± 2.86	105.44 ± 2.45
Stress @ Y (MPa)	28.82 ± 3.91	43.25 ± 3.21	60.77 ± 4.77	75.50 ± 11.44
Strain @ Y (%)	4.37 ± 1.45	5.08 ± 2.07	4.55 ± 0.30	3.65 ± 0.81
Strain Rate (sec <sup>-1</sup> )	.0096 ± 0.001	0.96 ± 0.03	118.20 ± 13.32	240.50 ± 5.65
Modulus (GPa)	1.21 ± 0.40	1.51 ± 0.57	2.34 ± 0.24	2.76 ± 0.22
Energy @ Y (MPa)	0.43 ± 0.25	0.86 ± 0.44	0.80 ± 0.12	1.18 ± 0.59

Table 5. XM39 Servohydraulic Compression Test Results.

	Nominal Strain Rate (sec <sup>-1</sup> )			
	10 <sup>-2</sup>	4x10 <sup>-2</sup>	1	100
Max. Stress (MPa)	28.26 ± 0.85	28.89 ± 0.61	39.65 ± 1.79	71.51 ± 2.18
Stress @ Y (MPa)	14.68 ± 1.27	18.84 ± 2.123	5.93 ± 2.60	55.93 ± 3.73
Strain @ Y (%)	2.77 ± 0.98	2.86 ± 0.56	3.66 ± 0.53	3.52 ± 0.22
Strain Rate (sec <sup>-1</sup> )	0.01 ± 0.0002	0.04 ± 0.0003	0.97 ± 0.02	104.60 ± 3.31
Modulus (GPa)	1.13 ± 0.35	1.08 ± 0.09	1.73 ± 0.04	2.98 ± 0.78
Energy @ Y (MPa)	0.12 ± 0.04	0.17 ± 0.07	0.49 ± 0.10	0.57 ± 0.17

250	
Max. Stress (MPa)	65.91 ± 7.92
Stress @ Y (MPa)	49.82 ± 15.06
Strain @ Y (%)	3.26 ± 1.92
Strain Rate (sec <sup>-1</sup> )	246.10 ± 8.50
Modulus (GPa)	3.07 ± 1.27
Energy @ Y (MPa)	0.37 ± 0.13

The compressive modulus (Figure 4) and the yield stress (Figure 5) both increase as a function of strain rate for all three propellants, yet the strain at yield remains relatively constant (Figure 6). Note that even though the moduli of M30 and XM39 are nearly identical, the strain energy density,  $\tau$ , absorbed at yield by the M30 propellant, is 2 and 5 times greater than that of XM39 and JA2 respectively (Figure 7). This observation could have important consequences for the design of new fracture resistant propellants as it appears that the triple base M30 propellant has higher yield stress levels than either the double base JA2 or single base XM39 propellants. However, visual inspection of deformed specimens of M30 and XM39 propellant reveals that macroscopic fractures develop in specimens tested at all strain rates above  $10^{-2} \text{ sec}^{-1}$ ; none of the JA2 specimens macroscopically fractured at any of the strain rates tested. Furthermore, rapid snapshots taken at 10 frames per second during the axial compression of specimens of XM39 reveal that macroscopic fractures begin to develop after about 2 seconds, or at 28 MPa and 7.7 percent axial strain. However, the stress and strain at yield determined using the minimum second derivative of stress with respect to time criterion indicates that the yield stress and strain occur at only 18.8 MPa and 2.9 percent respectively (Table 5). Since the appearance of macroscopic fractures does not correspond with macroscopic yield of the specimen, detailed microscopic observations are needed to define when microfracturing begins.

The average compressive moduli of M30, XM39, and JA2 at room temperature and a strain rate of  $250 \text{ sec}^{-1}$ , determined using the Servohydraulic Tester, compare well with the moduli determined using the Drop Weight Mechanical Properties Tester (Table 6). However, the stress versus strain responses considerably differ, particularly in the post-failure region for the work-softening M30 and XM39 propellants (Figures 8a and 8b). The difference in material response is attributed to the differing input strain histories between the devices. The input strain rate on the MTS is computer controlled and remains relatively constant throughout the deformation history. However, the strain rate on the DWMPT remains constant only to yield, then becomes zero, negative, and begins to increase again as the upper load piston rebounds off the specimen preparing for a second impact. Multiple ram impacts will reoccur until the total kinetic energy of the ram is dissipated in work done in deforming the propellant, and frictional and impact sound losses. Figure 8c illustrates a typical multiple impact response for JA2. Since the response is ductile, the post-yield stress-strain curves compare more favorably with that of the MTS since instabilities present during macroscopic failure are not present.

Table 6. A Comparison of Compressive Moduli Determined Using the MTS and DWMPT at Room Temperature and Strain Rate of  $250 \text{ sec}^{-1}$ .

	M30	XM39	JA2
DWMPT Modulus (GPa)	2.74	4.08	.782
MTS Modulus (GPa)	2.76	3.07	.790

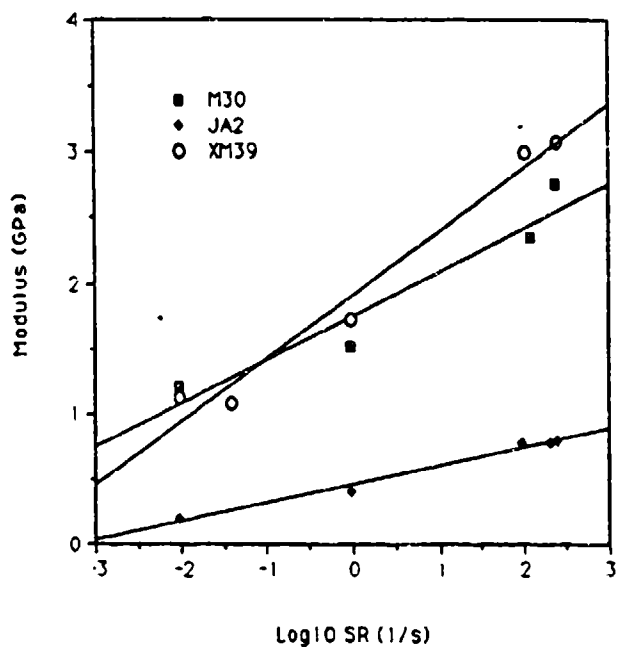


Figure 4. Modulus versus Strain Rate.

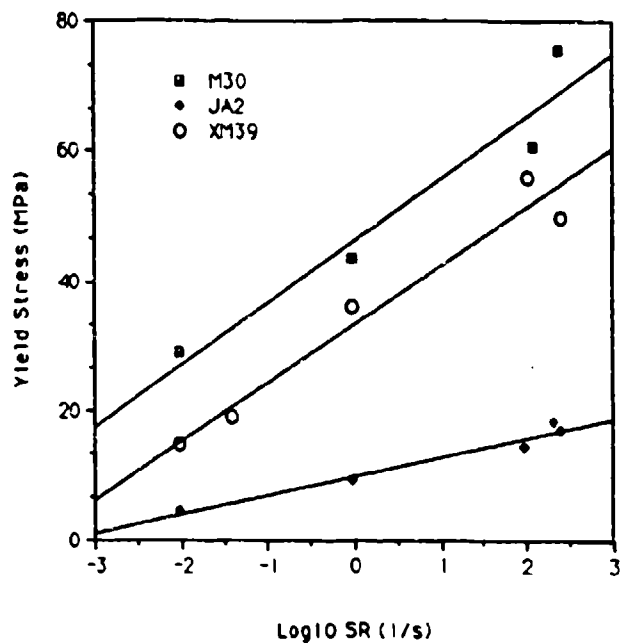


Figure 5. Yield Stress versus Strain Rate.

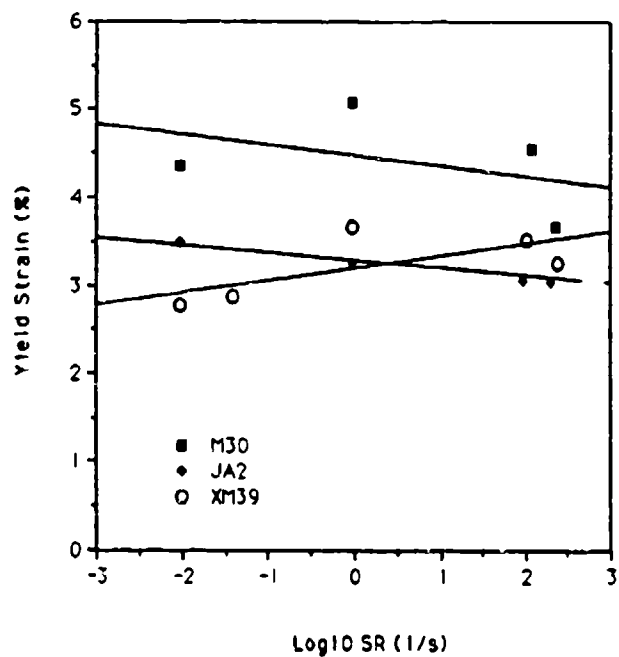


Figure 6. Yield Strain versus Strain Rate.

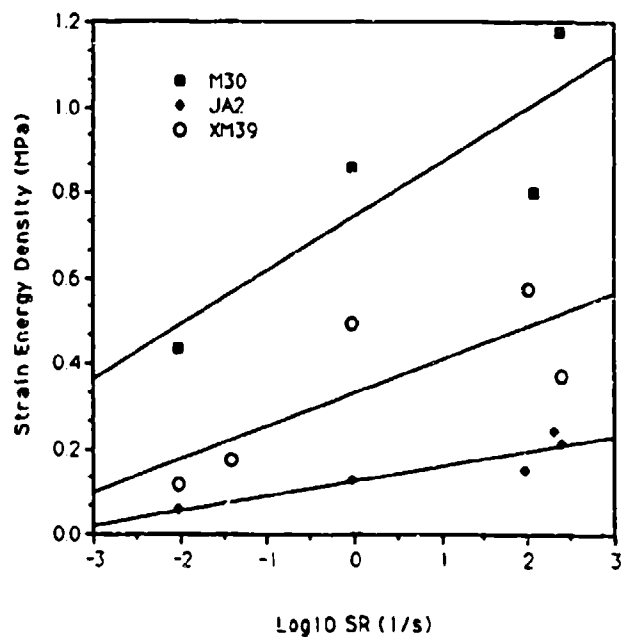


Figure 7. Strain Energy versus Strain Rate.

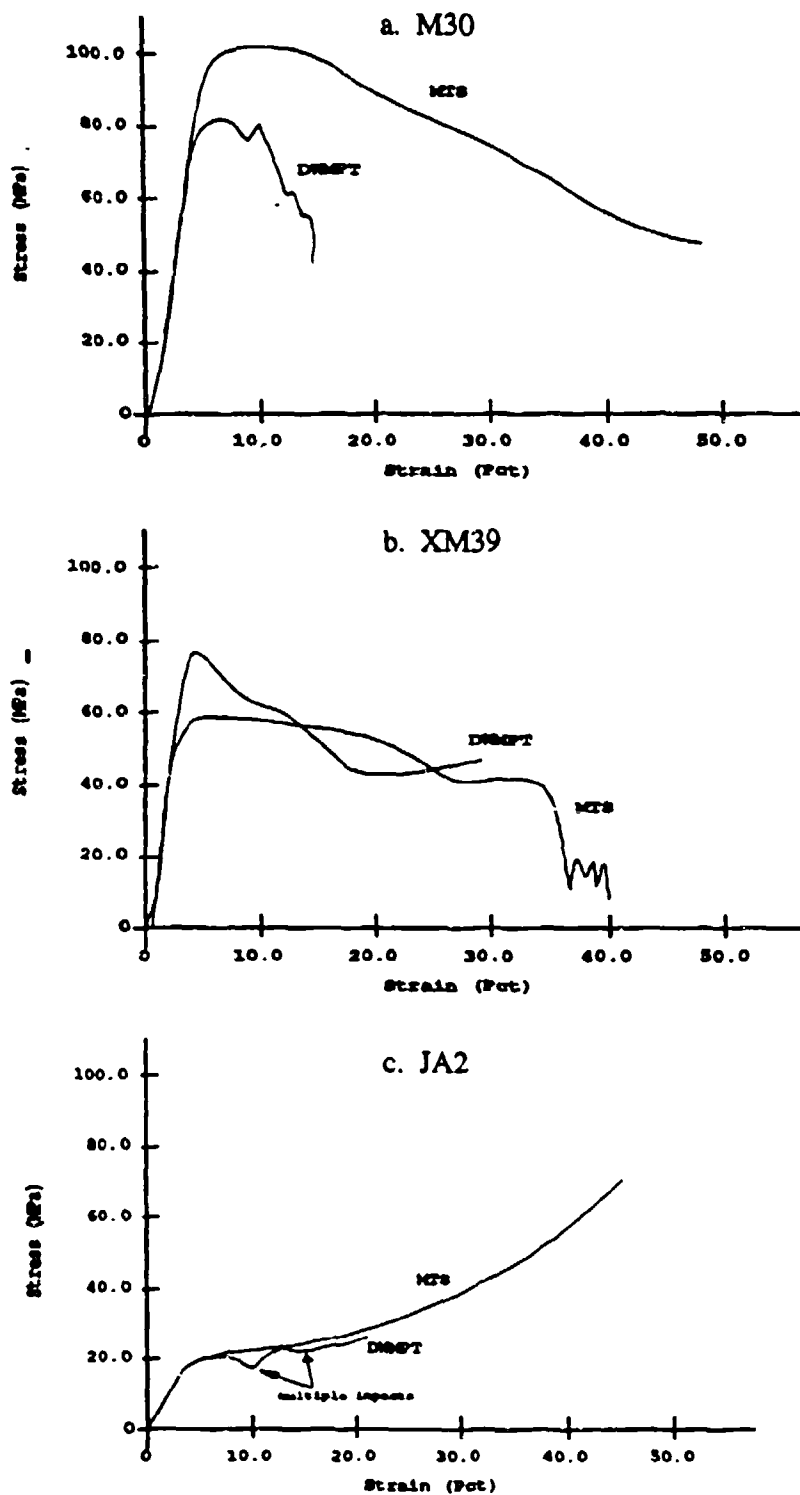


Figure 8. Representative Stress versus Strain Curves which Compare the Mechanical Response of M30, XM39, and JA2 Propellants at Room Temperature and a Strain Rate of  $250 \text{ sec}^{-1}$ .

## 5. ABSORBED STRAIN ENERGY DENSITY

5.1 Cumulative Absorbed Strain Energy Density. The cumulative strain energy density per unit volume,  $\tau$ , absorbed by M30, XM39, and JA2 propellants at increasing increments of strain (to 30 percent) versus strain rate are illustrated in contour maps and 3-dimensional surfaces (Appendix B). The cumulative strain energy density was greater for the work-softening M30 and XM39 propellants with maxima at 23 and 16 MPa respectively. This is because much higher stress levels were attained during the deformation of these materials. The maximum strain energy density for the work-hardening JA2 propellant is only 7 MPa at 30 percent strain. All three propellants are macroscopically ductile yet M30 and XM39 propellants fractured and work-softened and JA2 flowed and work-hardened during deformation. However, the macroscopic ductility in JA2 could be accommodated by a microphysical fracture deformation mechanism and future experiments carried to fixed amounts of total strain are planned in an effort to study the phenomenon.

5.2 Incremental Absorbed Strain Energy Density. The normalized incremental strain energy density,  $\Gamma$ , absorbed by M30, XM39, and JA2 propellants determined at increments between 0 and 10, 10 and 20, and 20 and 30 percent strain versus strain rate are illustrated in contour maps and 3-dimensional surfaces (Appendix C). The contours in these plots are normalized to the maximum cumulative strain energy absorbed as described in the previous section. The dimensionless  $\Gamma$  contour maps reveal that the M30 and XM39 propellants possess a saddle with maximum  $\Gamma$  of about .4, and strain increment between 10 and 20 percent. This behavior is expected since the stress strain curves for M30 and XM39 work-soften after the maximum stress has been reached. The  $\Gamma$  contour map for JA2, however, does not possess a saddle but continually increases; this behavior is also expected for macroscopically ductile work-hardening materials.

## 6. TIME DEPENDENT MECHANICAL PROPERTIES

The following section includes some initial results on the viscoelastic characterization of M30, XM39, and JA2 propellants. Since perforated specimens were tested, the measured response contains both structural and material contributions. It may be impossible to determine the intrinsic material properties for these materials since extruded propellants with multiple perforations possess a directional anisotropy not present in the solid material. Furthermore, the determination of constitutive equations for materials requires that the boundary value problem be homogeneous, viz., the stresses within the continuum be identical to those applied at the boundary. Real world testing conditions only approach this requirement, and in the final analysis the results of testing perforated specimens will be no better than for any material that contains large internal voids or pores.

**6.1 Linear Viscoelasticity Theory.** A material exhibits linear behavior in response to a generalized input if the following two conditions are satisfied:

$$1) R[I_a + I_b] = R[I_a] + R[I_b] \quad \text{Superposition Property}$$

$$2) R[cI] = cR[I] \quad \text{Homogeneity Property}$$

where  $I$ ,  $I_a$ , and  $I_b$  are general input histories and the brackets  $[ ]$ , are used to denote that the current value of  $R$  depends on the history of  $I$  and not just its instantaneous value. Following the notation of Schapery<sup>14,17</sup>, if a material is linear, the response  $R(t)$  to a general input  $I(t)$  can be written as:

$$R(t) = \int_{-\infty}^t R_H(t - \tau) \frac{dI}{d\tau} d\tau$$

The above relation connecting input and response is commonly referred to by various names such as, hereditary integral, superposition integral, Duhamel's integral, or convolution integral.  $R_H(t)$  is the unit response function for a nonaging material (viz. a material whose material properties do not depend on the time they are tested). In a creep test,  $R_H(t) = D(t) = \epsilon(t)/\sigma_0$  where  $D(t)$  is the creep compliance and is experimentally determined by performing a creep test while applying a constant stress input,  $I = \sigma_0 H(t)$  (Figure 9).  $H(t)$  is the Heaviside step function defined as:  $H(\arg) = 1$ ,  $\arg > 0$ ;  $H(\arg) = 0$ ,  $\arg < 0$ . In a relaxation test,  $R_H(t) = E(t) = \sigma(t)/\epsilon_0$  where  $E(t)$  is the relaxation modulus and is experimentally determined by performing a relaxation test while applying a constant strain input,  $I = \epsilon_0 H(t)$  (Figure 10).

Some common linear creep compliances that are often used in the literature include the power law  $D(t) = D_0 + D_1 t^m$ , and Maxwell  $D(t) = D_0 + t/\eta$  viscoelastic rheologies. Writing the convolution integral in terms of one-dimension yields for strain and stress:

$$\epsilon(t) = \int_{-\infty}^t D(t - \tau) \frac{dI}{d\tau} d\tau \quad (5)$$

$$\sigma(t) = \int_{-\infty}^t E(t - \tau) \frac{dI}{d\tau} d\tau \quad (6)$$

where  $D(t)$  is the creep compliance and  $E(t)$  is the relaxation modulus. Once the relaxation modulus is experimentally determined, the stress as a function of time is expressed for an arbitrary strain input with Equation 6. Equations 5 and 6 form the one-dimensional constitutive equations for a linear viscoelastic nonaging material.

**6.2 Constant Strain Rate Test.** The input for a constant strain rate test is given by:

$$\epsilon(t) = c t H(t) \quad (7)$$

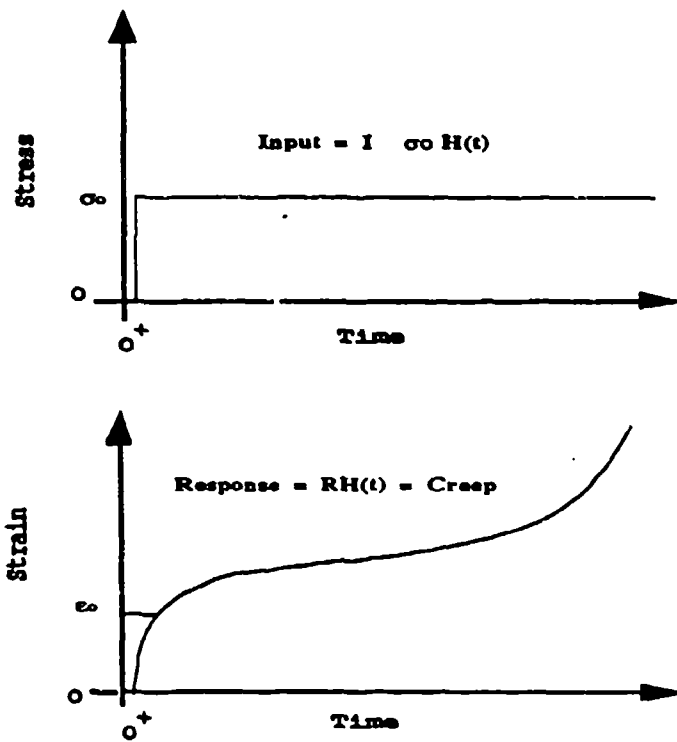


Figure 9. Creep Response to a Unit Input in Stress.

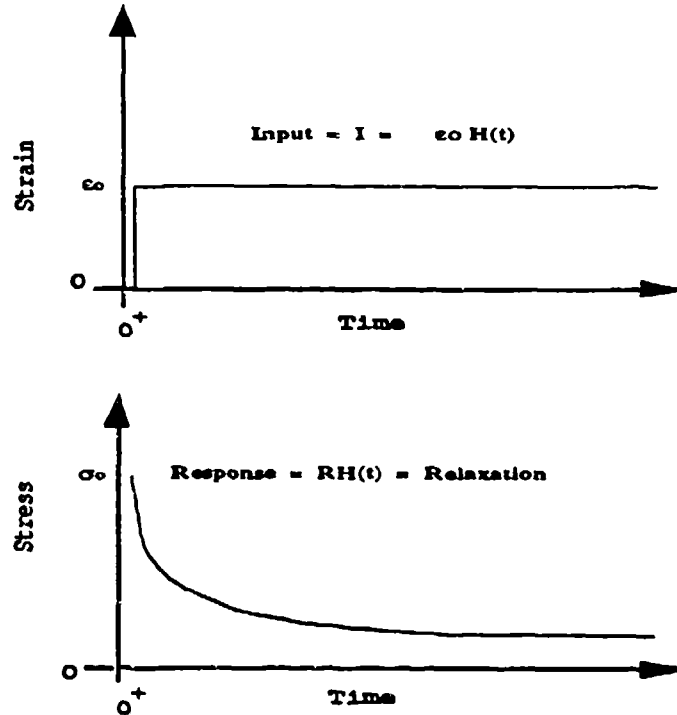


Figure 10. Relaxation Response to a Unit Input in Strain.

where  $c$  is the constant strain rate. Substitution of Equation 7 into Equation 6 with a change of variables  $u=t-\tau$ , and assuming that  $E(t-\tau) = 0$  for  $t < \tau$  gives:

$$\sigma(t) = c \int_0^t E(u) du \quad t > 0 \quad (8)$$

differentiating both sides of the Equation 8 with respect to time gives the relaxation modulus:

$$E(t) = d\sigma/d\varepsilon \quad (9)$$

This shows that the relaxation modulus is obtainable from a constant strain rate experiment and is equal to the tangent modulus, which is the local tangent to the stress versus strain curve taken at times,  $t = \varepsilon/c$ . It can also be shown that the relaxation modulus is related to the secant modulus, defined as:

$$E_s = \sigma/\varepsilon \quad (10)$$

The secant modulus can be written by substituting Equation 8 into Equation 10, which gives:

$$E_s = 1/t \int_0^t E(u) du \quad t > 0 \quad (11)$$

Differentiating both sides of Equation 11 and solving for  $E(t)$  gives:

$$E(t) = E_s + t \, dE_s/dt \quad (12)$$

Equation 12 can be written as:

$$E(t) = E_s [1. + (dE_s/E_s)/(dt/t)] \quad (13)$$

Using a property of logarithms<sup>14,15</sup> (i.e.  $\ln_{10} d(\log_{10} x) = dx/x$ ), Equation 13 can be rewritten as:

$$E(t) = E_s [1. + d(\log_{10} E_s)/d(\log_{10} t)] \quad (14)$$

Note that if the slope of the  $\log E_s$  versus  $\log t$  curve is much less than one, then the relaxation modulus,  $E(t)$ , is nearly identical to the secant modulus,  $E_s$ . Furthermore, since both  $E(t)$  and  $E_s$  are both functions only of time, if any strain level dependence is observed the material is nonlinear.

To determine the relaxation moduli, secant moduli and to test for linear/nonlinear viscoelastic behavior for the M30, XM39, and JA2 propellants, we use the constant strain rate data and plot the log of the secant modulus (Equation 10) versus log time (Appendix D). The time is determined by  $t = \varepsilon/c$ , where  $\varepsilon$  is the fixed strain level and  $c$  is the strain rate. As an example, the relaxation and secant moduli are determined from the JA2 test data taken at different strain rates (Figure 11) and plotted as a function of time at strain levels of 5, 10, 20 and 30 percent in Figure D1. The lines in Figure D1 represent the moduli determined at different strain levels as defined by the symbols in Figure 11. By using data taken from several tests over a wide range of strain rates, the relaxation



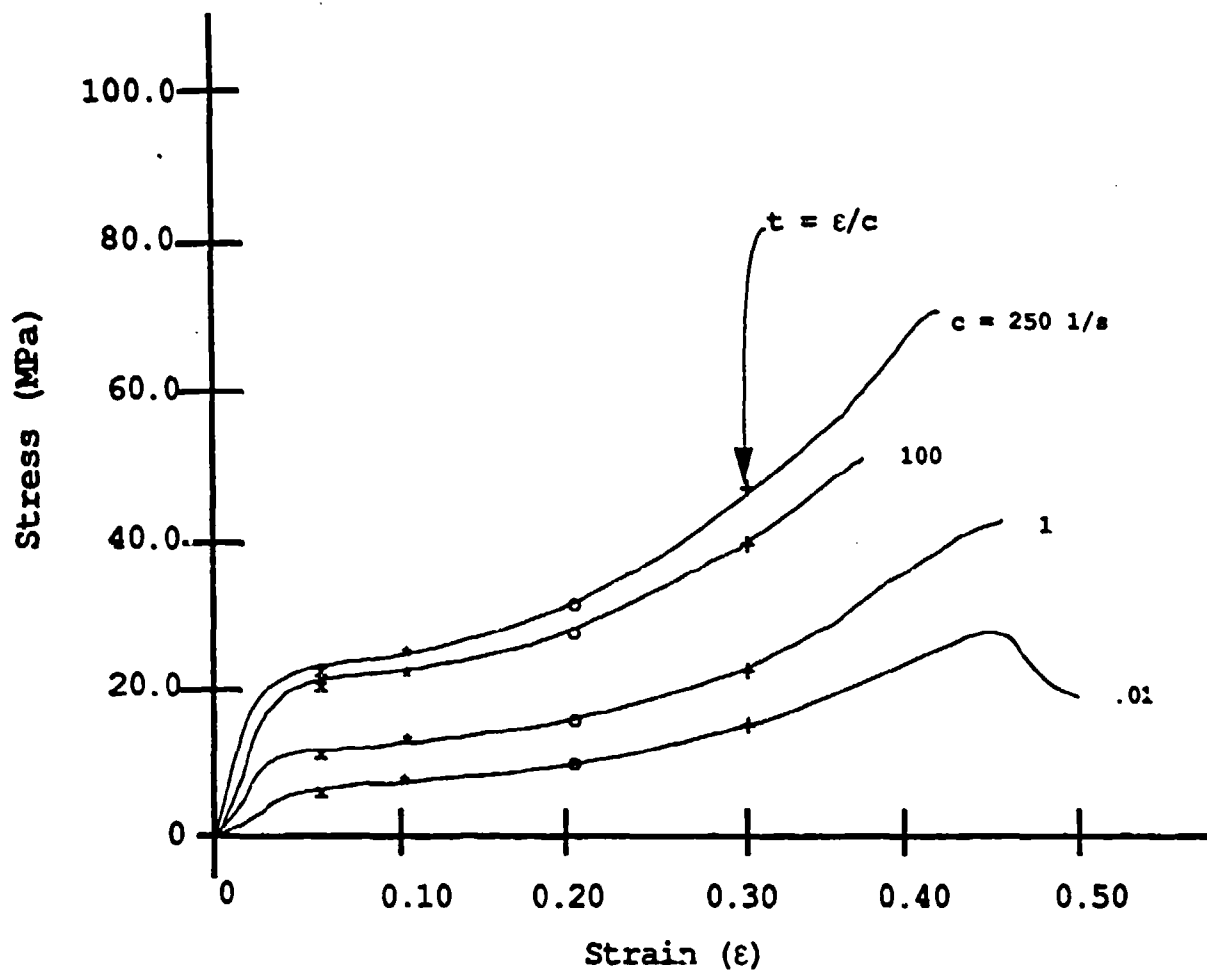


Figure 11. Graphical Means for Determining Relaxation Moduli (Appendix D) for IA2 Tested at Various Strain Rates.

and secant moduli can be determined for the material for times which range over many orders of magnitude. All three propellants exhibit a strong nonlinear response as evidenced by the strain level dependence of the secant modulus. The slopes of the  $\log E_t$  versus  $\log t$  curves are much less than one, so the relaxation modulus (dashed lines in Appendix D) can be well represented by the secant modulus. Data from the Split Hopkinson Bar are also included and indicate good experimental agreement with secant moduli determined over a wide range of strain rates from  $10^{-2}$  to  $10^{-4}$ . The room-temperature relaxation modulus for these propellants can be represented by a power-law of the form:

$$E(t) = E_1 t^n \quad (15)$$

Laplace transforms can be used to show that a good approximation of the creep compliance is:

$$D(t) = E(t)^{-1} \quad (16)$$

which is in error by at most 10 % when  $0 < n < .25$  in Equation 15<sup>14</sup>. For linear materials, the relaxation and creep compliances are directly substituted into Equations 5 and 6, and the one-dimensional stress and strain response for the propellant can be determined for any arbitrary stress or strain input history. This procedure cannot be applied for nonlinear functionals however, but can be treated using the multiple integral representations of nonlinear viscoelasticity<sup>16</sup> or an alternative formulation<sup>17</sup> whereby the relaxation moduli are vertically shifted to form "master" curves. This procedure is similar to the horizontal time-temperature shifting procedure performed on thermorheologically simple materials<sup>14</sup>.

## 7. SUMMARY AND CONCLUSIONS

This report describes the preliminary results of a series of mechanical property tests for the room temperature, uniaxial compression of M30, XM39, and JA2 gun propellants at strain rates of .01, 1, 100, and 250 per second using the Ballistic Research Laboratory's new High Rate servohydraulic test apparatus.

Using a linear elastic model, the apparatus stiffness is determined to be about 92 kN/mm. The strain energy absorbed at yield for a "typical" propellant grain is 7 times greater than the energy stored in the apparatus, so that the complete post-failure stress versus strain curve can be traced using the servohydraulic test apparatus. The compressive moduli determined with the servohydraulic apparatus compare favorably with those determined using the Drop Weight test apparatus at a strain rate of 250 per second. However, the post-failure behaviors of M30 and XM39 tested on these apparatuses do not compare well, and are probably a consequence of differing input strain histories imparted to the specimens on each of the apparatuses in the post-failure regime. This hypothesis might be verified by simulating a strain history input from a typical Drop Weight test on the servohydraulic apparatus, and observing whether the post-failure responses are comparable.

The compressive modulus, yield stress, and absorbed strain energy at yield all increase for these propellants as a function of strain rate, whereas the yield strain remains relatively constant and independent of strain rate. The M30 and XM39 propellants macroscopically failed by fracture at all strain rates tested. The JA2 propellant did not fracture but macroscopically flowed during the entire

deformation history. Microfracturing could be a mechanism for macroscopic flow and ductility so that detailed microstructural observations are necessary to determine when and if fracturing begins, since it is at this time that additional surface area becomes available for burning.

A preliminary viscoelastic characterization indicates that all three propellants exhibit nonlinear behavior. Since the specimens contain perforations, both a structural and material contribution to the nonlinearity is present. In order to obtain stress homogeneity within specimens, testing for constitutive properties is normally performed on solid specimens. This may not be valid for propellants since the extrusion process imparts a directional anisotropy oriented along the grain axis not present in solid grains. For the present then, we will consider these tests as "pseudo" constitutive tests, the results of which are no better than any material which contains voids, large pores or other internal inhomogeneities.

The room temperature secant and relaxation moduli for these propellants can be represented by a power law in time for strain rates which range from  $10^{-2}$  to  $10^{-4}$   $\text{sec}^{-1}$ . The relaxation moduli determined from tests at strain rates greater than  $250 \text{ sec}^{-1}$  are obtained from Split Hopkinson Bar tests<sup>5</sup> and are linearly extrapolatable from the servohydraulic test results conducted at lower strain rates.

## 8. FUTURE WORK

**8.1 Microstructural Observations.** Future work should focus on detailed scanning electron microscope and optical microscope observations of the deformation mechanisms to determine when microfracturing begins to occur in these propellants. A vacuum impregnation epoxy technique might be used to help maintain grain integrity, since these propellants are relatively soft and can be damaged during preparation for optical examination. The technique has been used for examining deformation mechanisms in crystalline materials and involves vacuum impregnating deformed specimens with dyed epoxy, hardening, and finally thin-sectioning and polishing the specimens. Tests where specimens are deformed to fixed amounts of total strain will permit the characterization of microstructural changes within the propellant, and determine when and under what conditions fractures begin to form. Mini closed-bomb tests should also be an integral part of the testing program, so that we can correlate the combustion characteristics of propellants, deformed to fixed amounts of total strain, to the macroscopic mechanical property parameters determined from the stress versus strain curves.

**8.2 Interior Ballistics Modeling.** Interior ballistics modeling will require data which characterize both the constitutive properties and a generalized failure criterion for propellants. A nonlinear viscoelastic constitutive characterization of the propellant which includes a damage model is presently being developed; a generalized failure criterion based on stress or strain invariants will require tests performed in compression, tension and torsion. The development of a generalized failure criterion is necessary since propellant grains are subjected to combined stress states within the gun cartridge during the ballistic cycle.

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**APPENDIX A:  
REPRESENTATIVE STRESS VERSUS STRAIN  
RESPONSE FOR JA2, M30, AND XM39**

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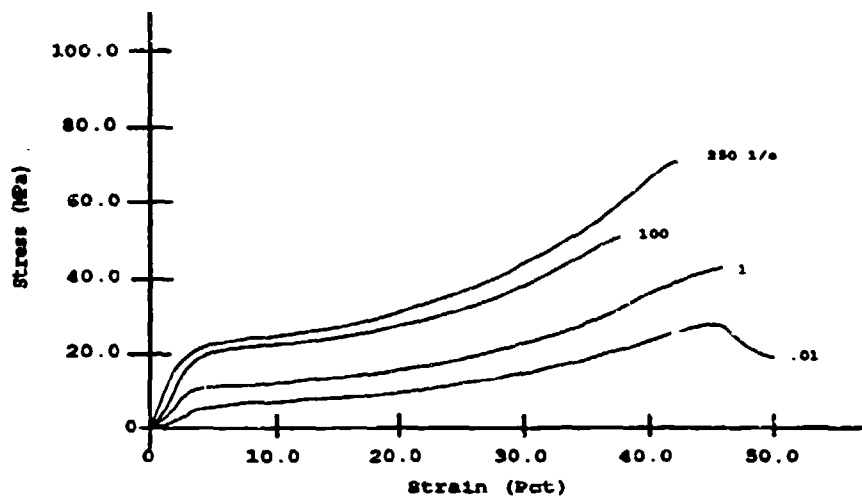


Figure A1. Representative Stress versus Strain Response for JA2

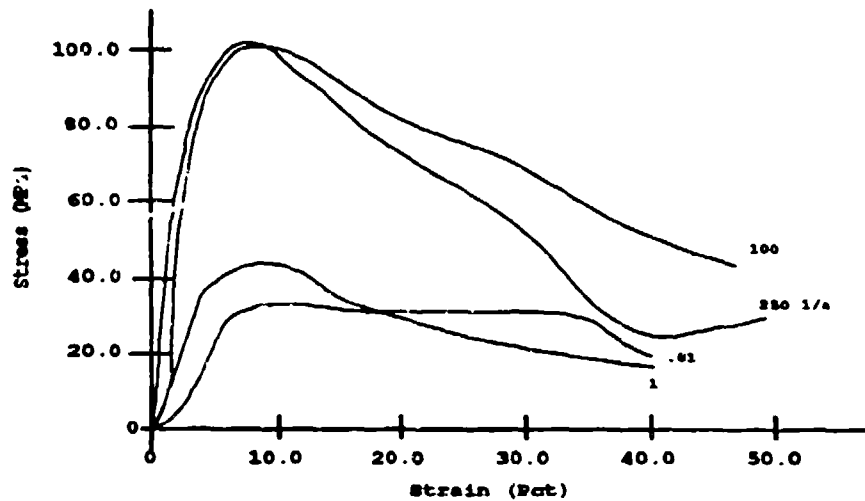


Figure A2. Representative Stress versus Strain Response for M30

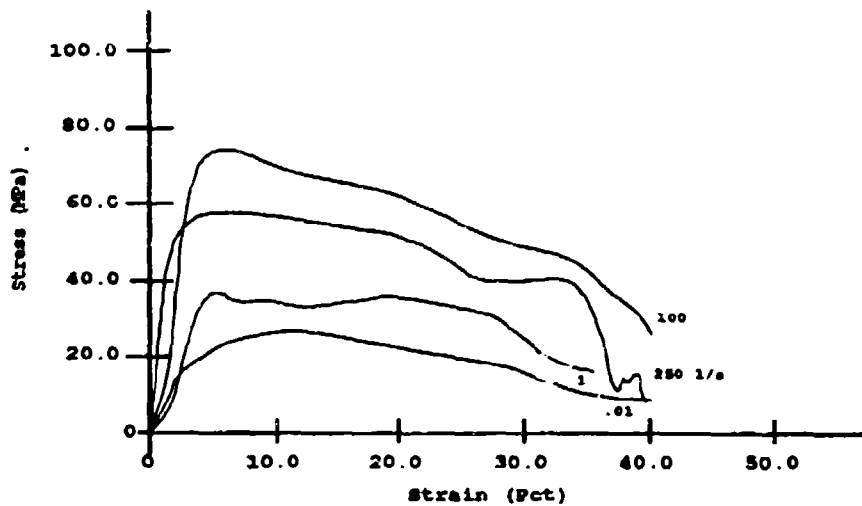


Figure A3. Representative Stress versus Strain Response for XM39

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**APPENDIX B:**  
**CUMULATIVE ABSORBED STRAIN ENERGY DENSITY MAPS**

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Figure B1. Cumulative Absorbed Strain Energy Density Map for **JA2**

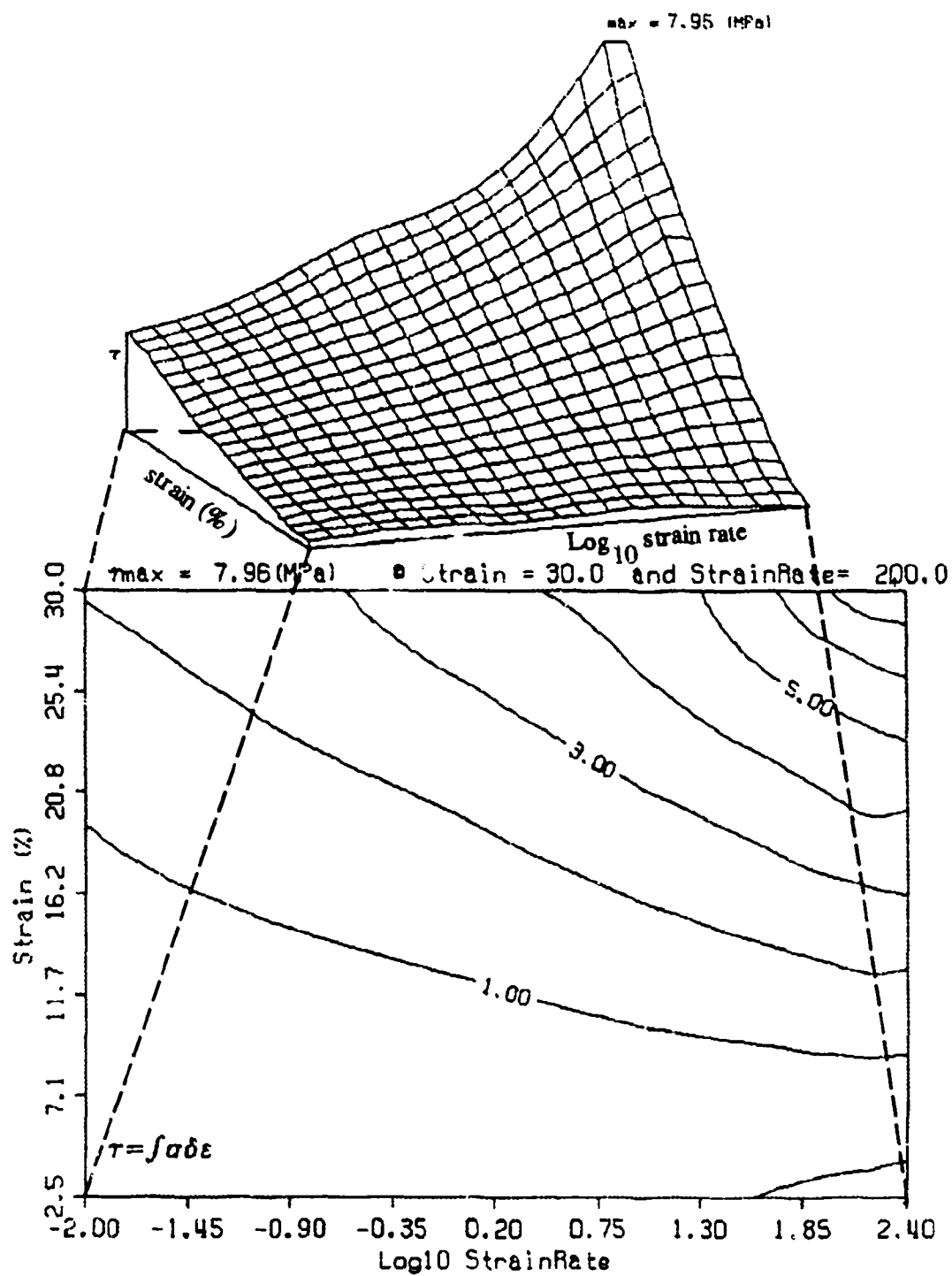


Figure B2. Cumulative Absorbed Strain Energy Density Map for **M30**

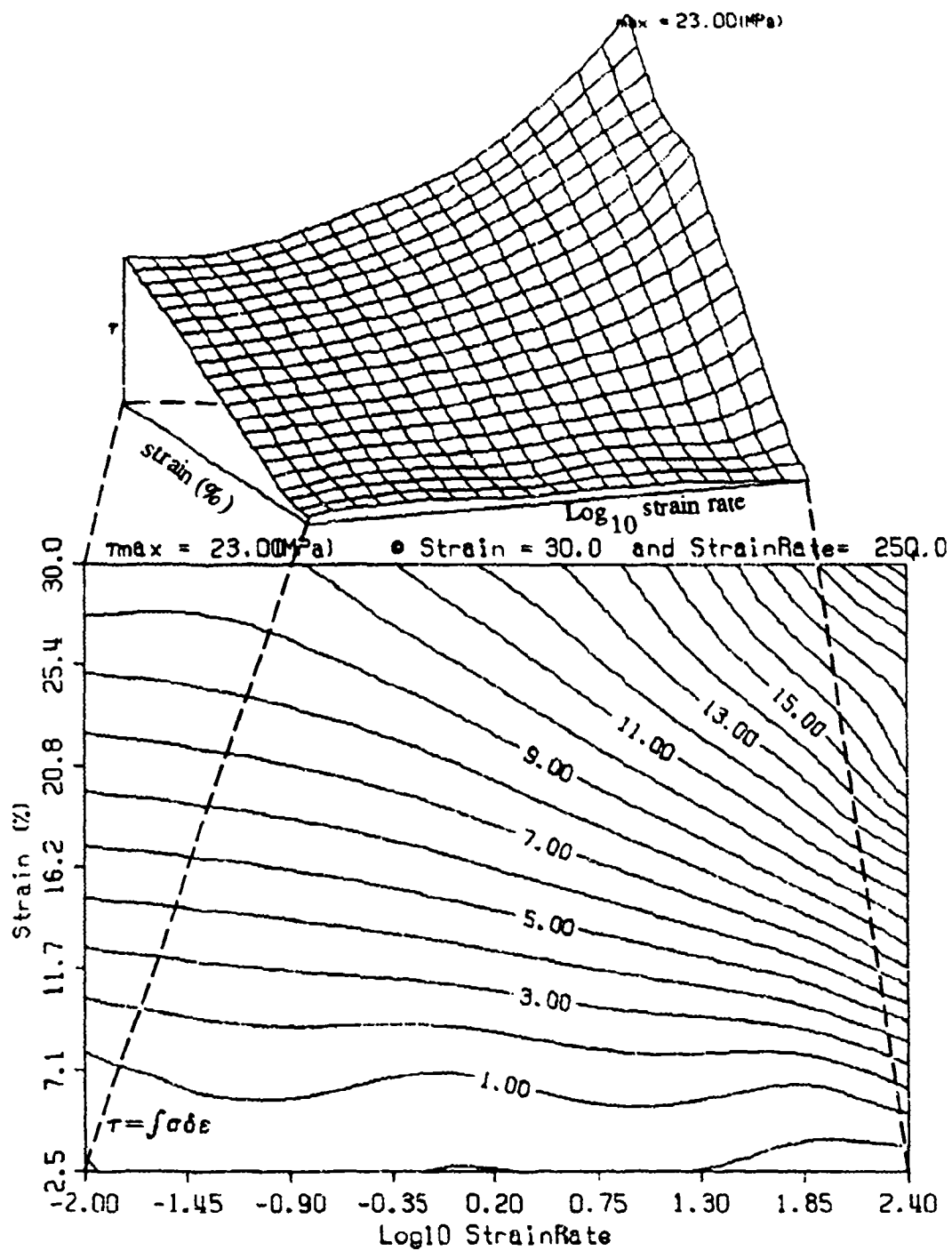
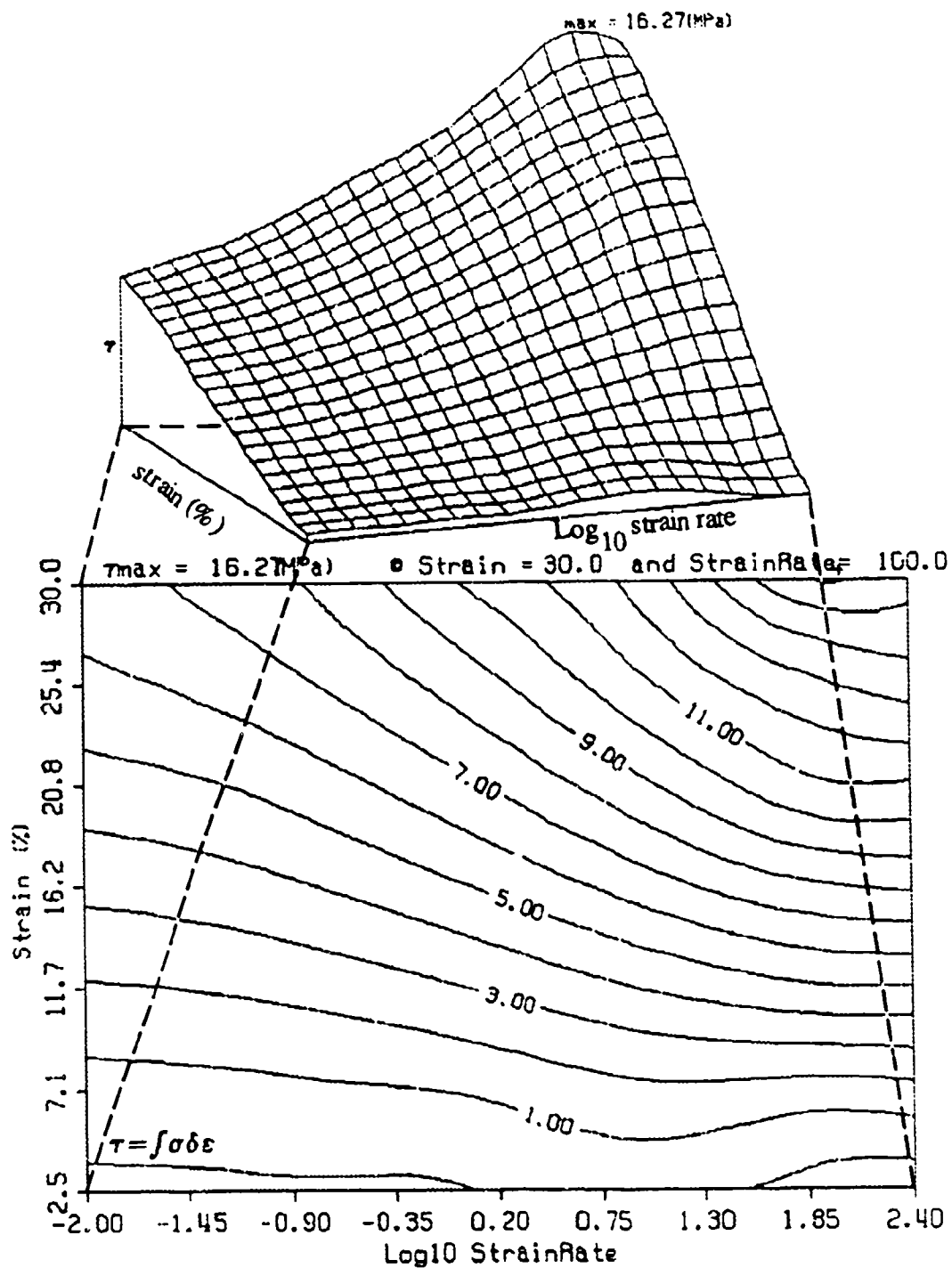


Figure B3. Cumulative Absorbed Strain Energy Density Map for **XM39**



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APPENDIX C:  
INCREMENTAL ABSORBED STRAIN ENERGY DENSITY MAPS

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Figure C1. Incremental Absorbed Strain Energy Density Map for JA2

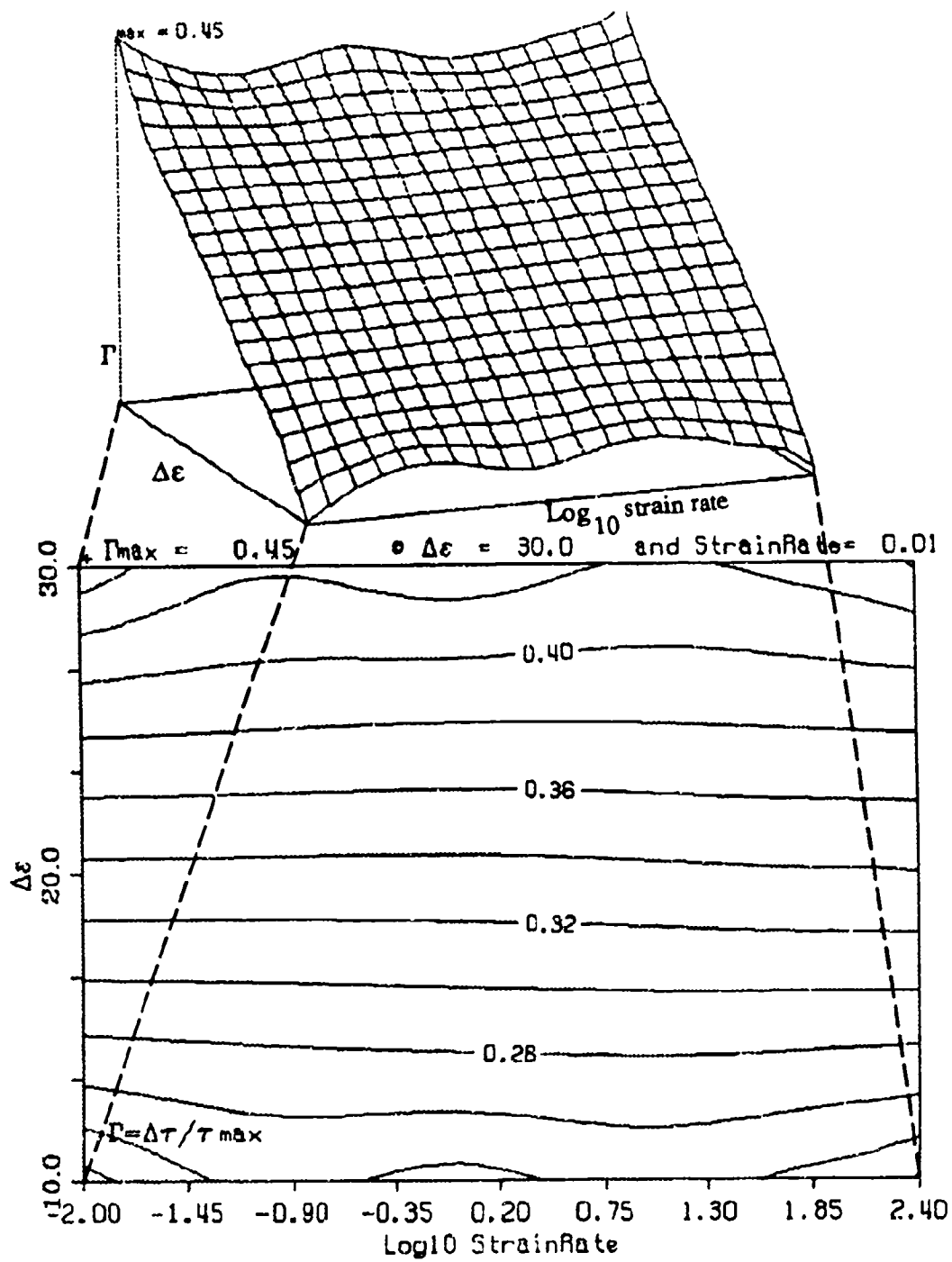


Figure C2. Incremental Absorbed Strain Energy Density Map for **M30**

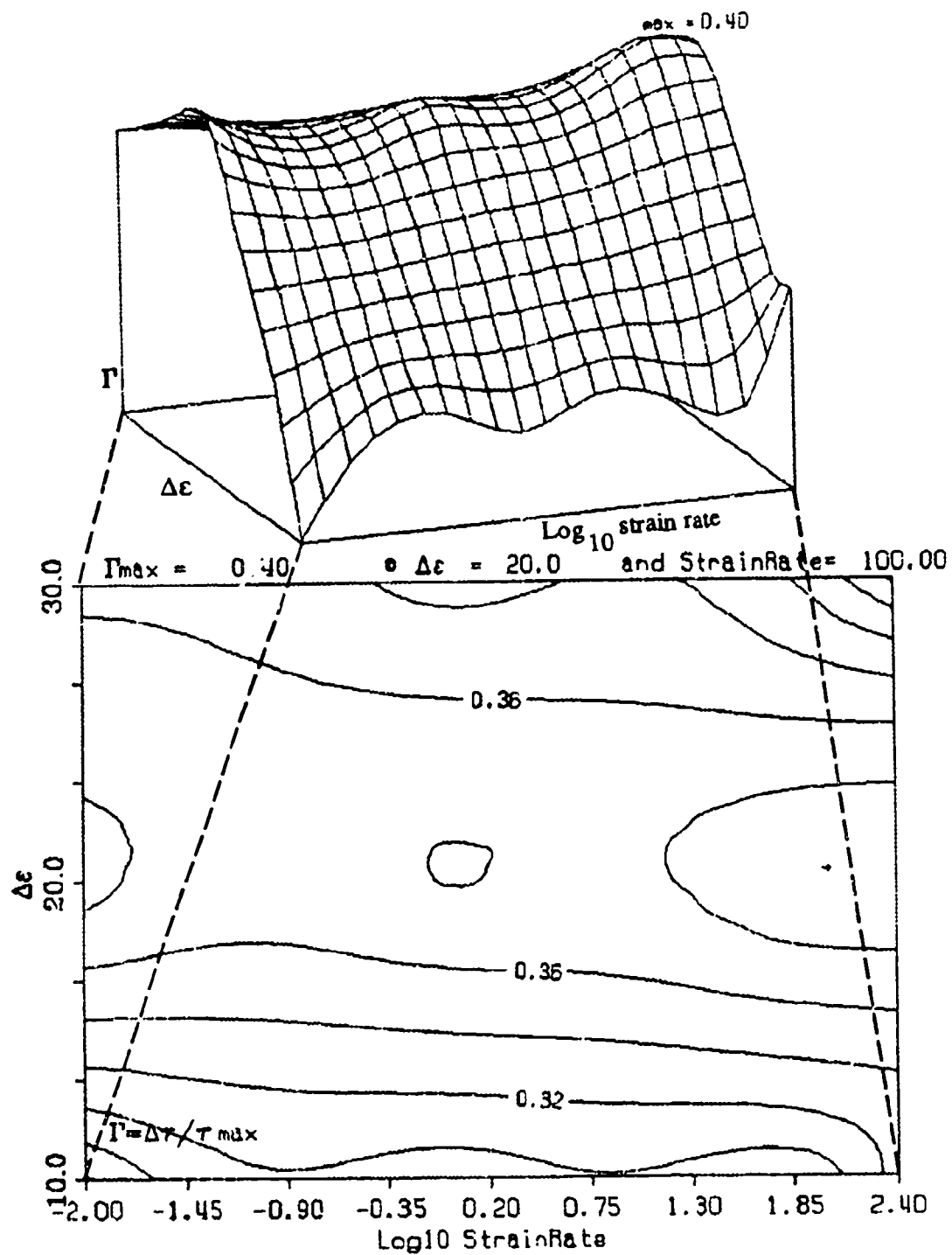
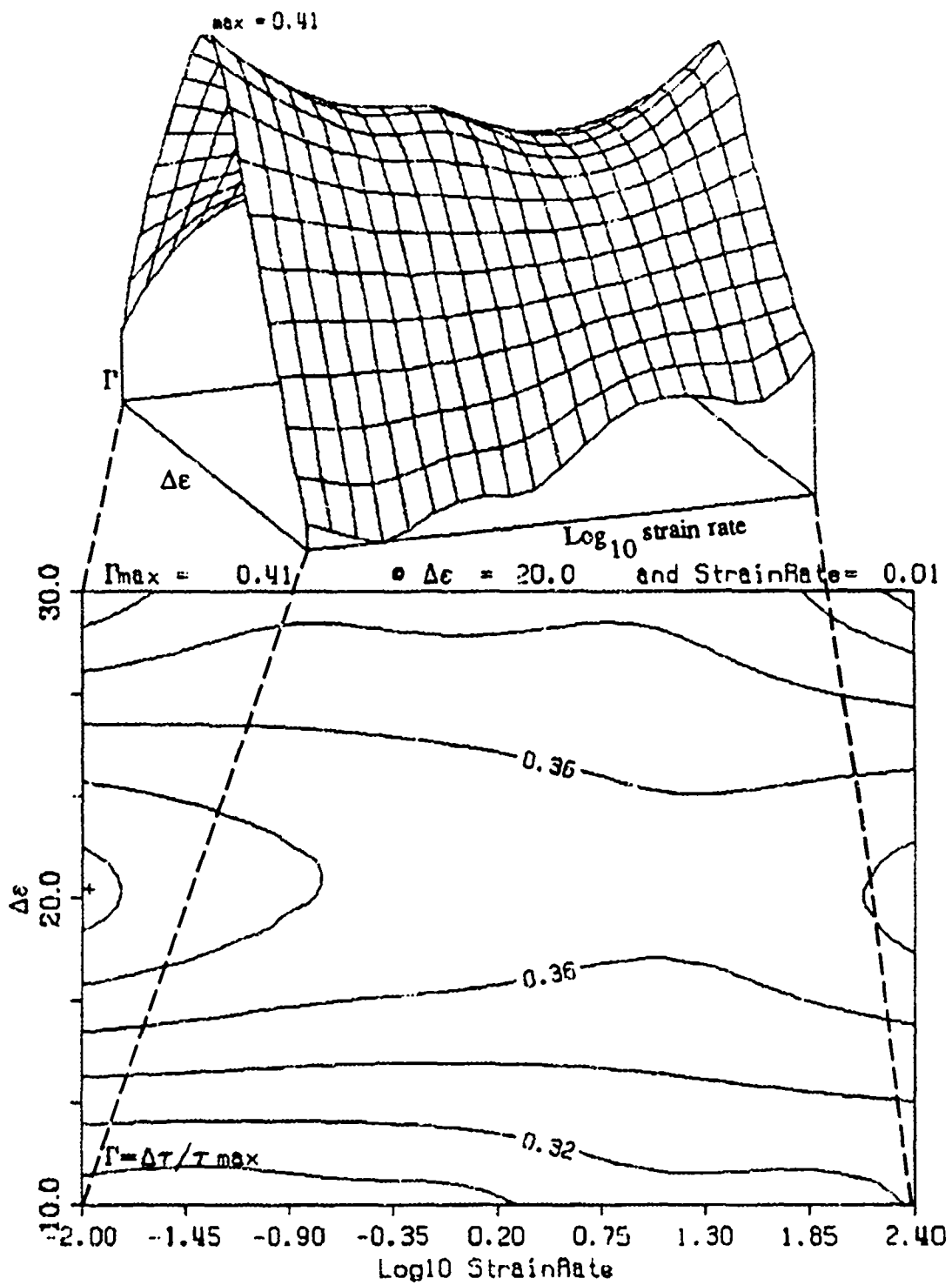


Figure C3. Incremental Absorbed Strain Energy Density Map for **XM39**



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**APPENDIX D:**  
**RELAXATION MODULI FOR JA2, M30, AND XM39 PROPELLANTS**

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Figure D1. JA2 Relaxation Moduli

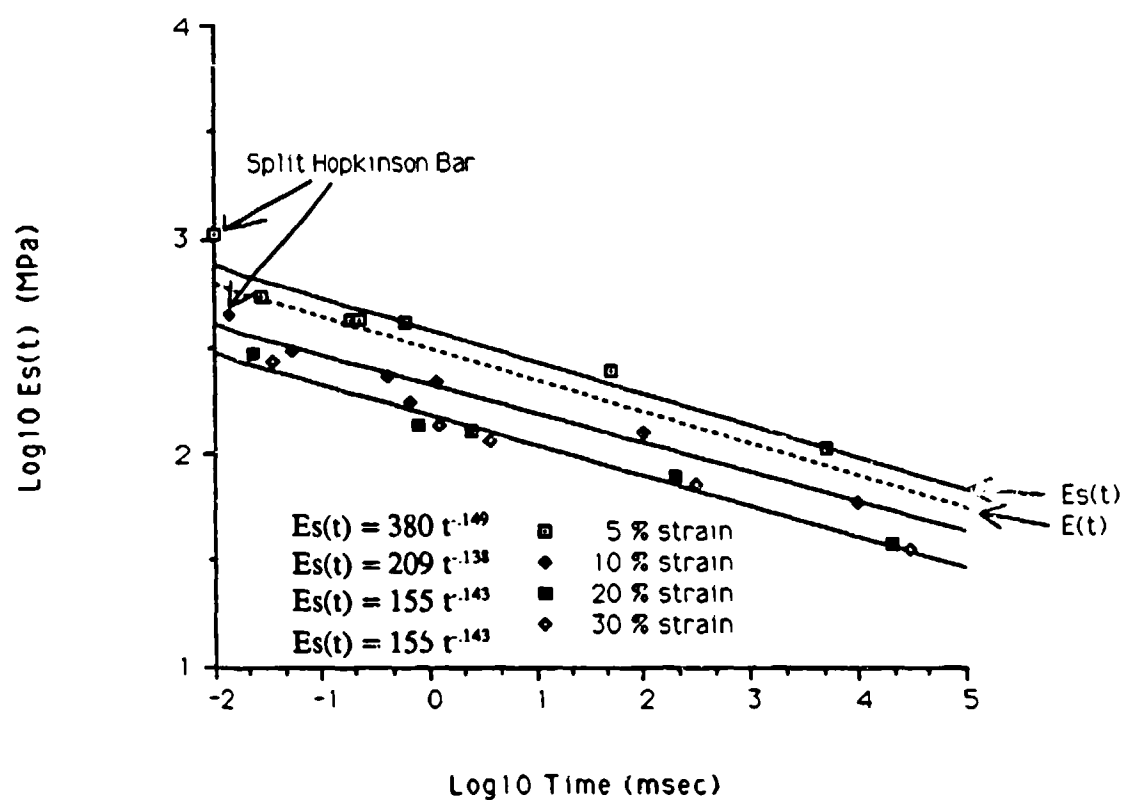


Figure D2. M30 Relaxation Moduli

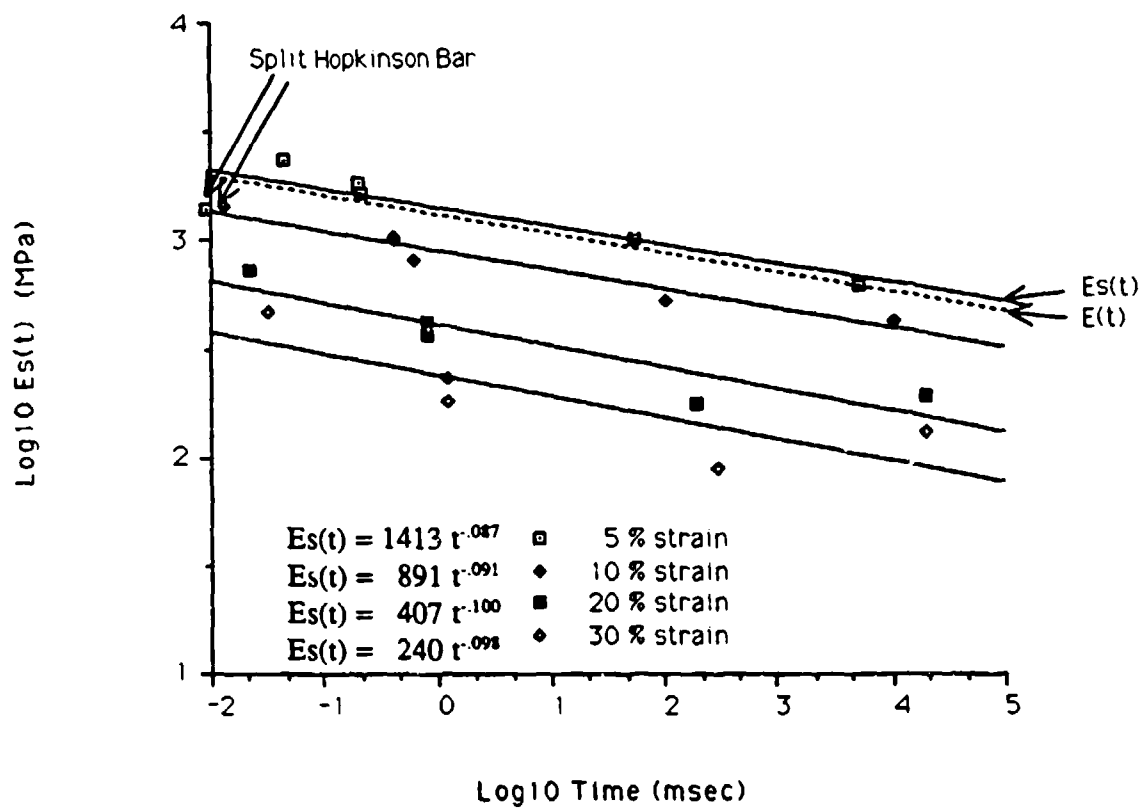
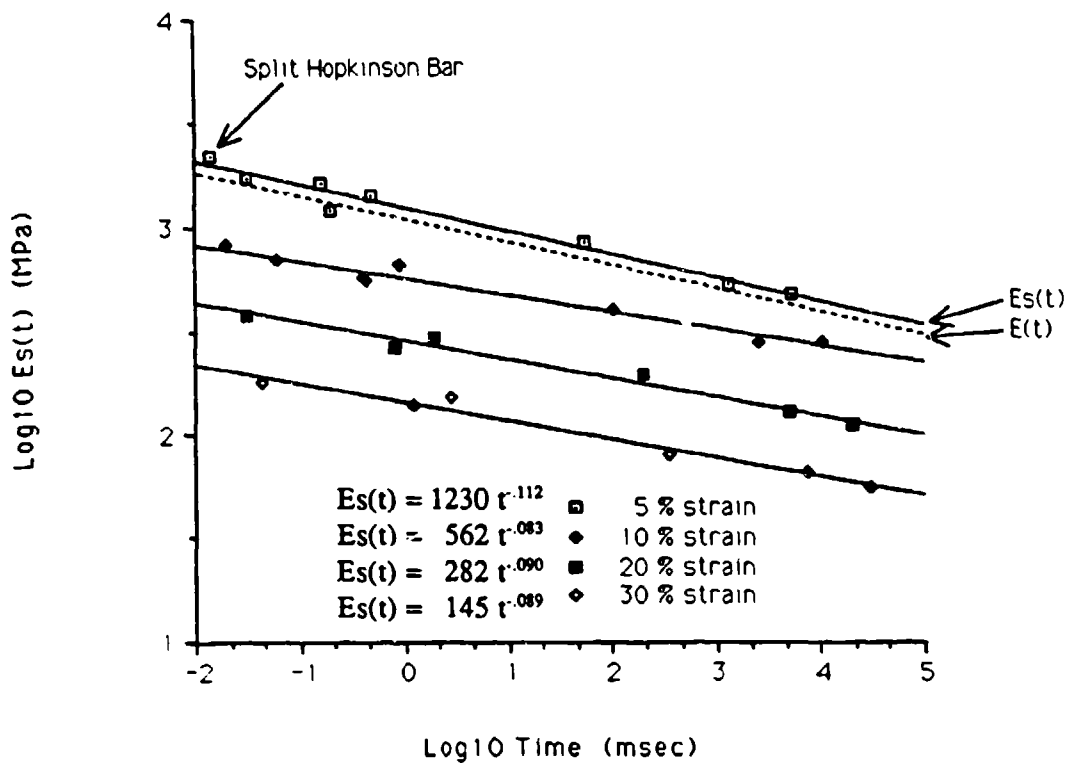


Figure D3. XM39 Relaxation Moduli



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